Chapter 29 – Electromagnetic Induction

Induction is critical to modern industrial life. It is the basis of generators and many motors. Without it light would not exist and thus life would not exist.

Goals for Chapter 28

- Study the magnetic field generated by a moving charge
- Consider magnetic field of a current-carrying conductor
- Examine the magnetic field of a long, straight, current-carrying conductor
- Study the magnetic force between currentcarrying conductors
- Consider the magnetic field of a current loop
- Examine and use Ampere's Law

Goals for Chapter 29

- Faraday's Law
- Lenz's Law
- Motional emf
- Induced electric fields
- Maxwell's equations and see their application to displacement current

Introduction

- The motion of a magnet can induce current in practical ways. If a credit card has a magnet strip on its back, "swiping" the card can generate tiny currents that send information to cash registers.
- A coil of wire and magnets set into motion around each other will generate currents in the wire. A source of mechanical energy can drive the rotation and make a waterfall into an electrical power station.



Induced current

 Joseph Henry worked in the United States and Michael Faraday worked in England to discern the details of current generated in wire and permanent magnets in motion relative to each other.



Knowing the magnetic flux

Regardless of what moves, knowing the magnetic flux around a conducting entity will allow determination of current induced.

Surface is face-on to magnetic field:

- \vec{B} and \vec{A} are parallel (the angle between \vec{B} and \vec{A} is $\phi = 0$).
- The magnetic flux $\Phi_B = \vec{B} \cdot \vec{A} = BA$.



Surface is tilted from a face-on orientation by an angle ϕ :

- The angle between \vec{B} and \vec{A} is ϕ .
- The magnetic flux $\Phi_B = \vec{B} \cdot \vec{A} = BA \cos \phi$.





Magnetic flux through element of area $d\vec{A}$: $d\Phi_B = \vec{B} \cdot d\vec{A} = B_{\perp} dA = B dA \cos \phi$

Surface is edge-on to magnetic field:

- \vec{B} and \vec{A} are perpendicular (the angle between \vec{B} and \vec{A} is $\phi = 90^{\circ}$).
- The magnetic flux $\Phi_B = \vec{B} \cdot \vec{A} = BA \cos 90^\circ = 0.$



EMF and the current induced in a loop

 A changing magnetic field induces an electric field – here the electric field is changing as well



Finding the direction of an induced emf

Induced EMF will produce current to create a magnetic field to OPPOSE the CHANGE in the original magnetic field



- Flux is positive ($\Phi_B > 0$) ...
- ... and becoming more positive $(d\Phi_B/dt > 0)$.
- Induced emf is negative ($\mathcal{E} < 0$).



- Flux is positive ($\Phi_B > 0$) ...
- ... and becoming less positive $(d\Phi_B/dt < 0)$.
- Induced emf is positive ($\mathcal{E} > 0$).



- ... and becoming more negative $(d\Phi_B/dt < 0)$.
- Induced emf is positive ($\mathcal{E} > 0$).



- Flux is negative ($\Phi_B < 0$) ...
- ... and becoming less negative $(d\Phi_B/dt > 0)$.
- Induced emf is negative ($\mathcal{E} < 0$).

Faraday's Law



Generator example

- A changing magnetic flux is actually what induces a changing electric field.
- Magnetic flux change is the field changes or if the direction changes



Generator example II

- In a sense a DC generator is a motor run in reverse
- Back EMF in a motor.
- Motor back EMF ultimately limits the motor speed
- Back EMF reduces voltage available to drive the motor
- Hence the motor current is less with speed torque drops



Generator example III

- A linear motor is similar to a rotary motor but is linear
- A "rail gun" is an example



Work and power in a slidewire generator

• A linear motor run backwards is a generator



Lenz's Law

• The direction of any magnetic induction effect is such as to oppose the cause of the effect.



The induced magnetic field is *upward* to oppose the flux change. To produce this induced field, the induced current must be *counterclockwise* as seen from above the loop.

The induced magnetic field is *downward* to oppose the flux change. To produce this induced field, the induced current must be *clockwise* as seen from above the loop.

A conducting rod moving in a uniform magnetic field

• The rod, velocity, and current are mutually perpendicular



(b) Rod connected to stationary conductor



The motional emf \mathcal{E} in the moving rod creates an electric field in the stationary conductor.

The Faraday Disk dynamo

- Solid metal disk in a static B field
- What breaks the symmetry in this problem = rotation
- Eddy Current = electronic brakes



Induced electric fields I

• The windings of a long solenoid carrying a current I



Induced electric fields II

- Practical examples of induction
- It is in your everyday life



- Hard disks read and write
- Motors in electric cars and hybrids regenerative breaking
- Ignition in gas engines

Eddy currents

- Metal detection •
- Airport and music store •
- Eddy current braking





Displacement current and Maxwell's equations

- A varying electric field will give rise to a magnetic field.
- A varying magnetic field gives rise to an electric field
- Thus -> electromagnetic waves.



Superconductivity and the Meissner effect

- When cooled below the critical temperature, superconductive materials lose all resistance to electrical current.
- Mercury was the first superconductor found
- We now have superconductors up to 140 K
- Perhaps room temperature superconductors will be found

(b) The temperature is lowered to $T < T_c$, so the material becomes superconducting.

Magnetic flux is expelled from the material, and the field inside it is zero (Meissner effect).

(c) When the external field is turned off at $T < T_c$, the field is zero everywhere.

